

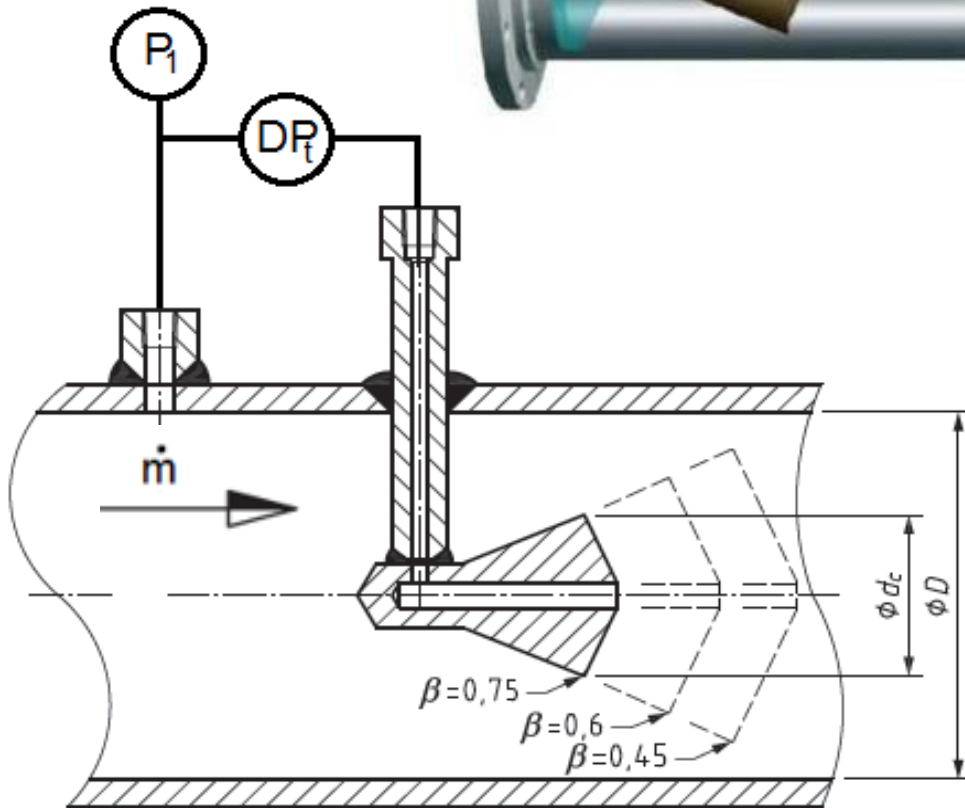
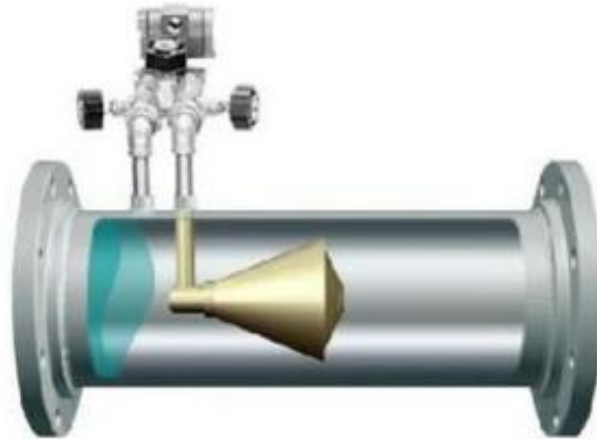
# CFD Modelling and Validation of a Cone meter

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# Cone Meter Background



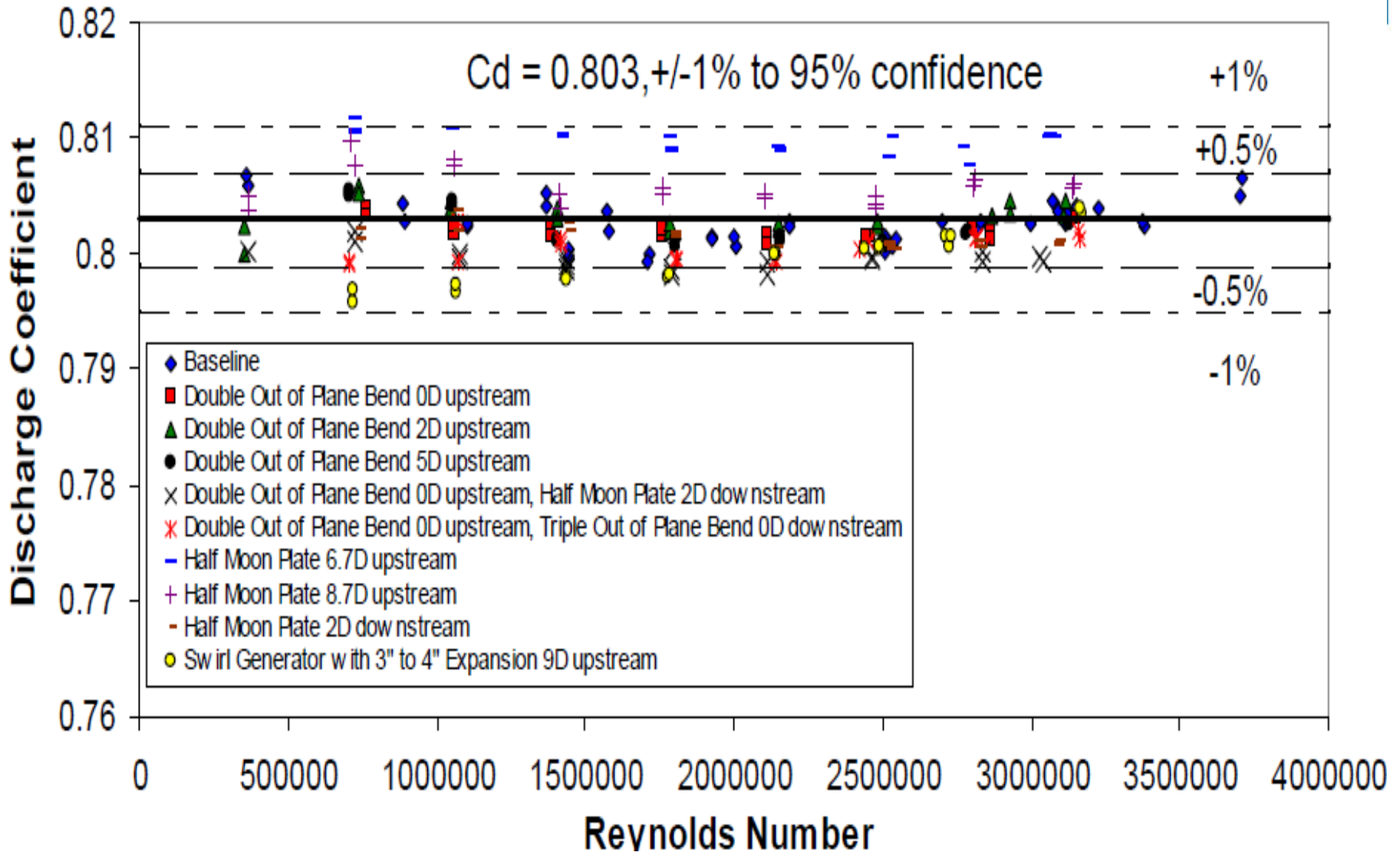
$$m_{actual} = C_d E A_t \varepsilon \sqrt{2\rho\Delta P}$$

$$E = \frac{1}{\sqrt{1-\beta^4}} \quad \beta = \sqrt{1 - \left(\frac{d_c}{D}\right)^2}$$

$$\varepsilon = 1 - \left(0.649 + (0.696\beta^4)\right) \left(\frac{\Delta P}{\gamma P_1}\right)$$

$$C_d = f(Re) = f\left(\frac{\rho\bar{U}D}{\mu}\right)$$

# Cone Meter Characteristics



# Presentation Objectives

- **Can you calibrate a Cone meter using CFD ?**
  - Investigate CFD prediction of Cone  $C_d$  accuracy of RANS based approaches.
  - Investigate Reynolds number effects

## Methodology

- Use the FLUENT 16 CFD code
- Compare directly with CEESI Meter Cone Test data

# Previous Validation Studies

- **Singh**– limited Reynolds number range- RANS- $k\epsilon$  models  
 $\approx 4\%$  accuracy

R. Singh, S. Singh and V. Seshadri, “Study on the effect of vertex angle and upstream swirl on the performance of a V Cone Flow meter using CFD,” *Flow Measurement and Instrumentation*, no. 20, pp. 69-74, 2009

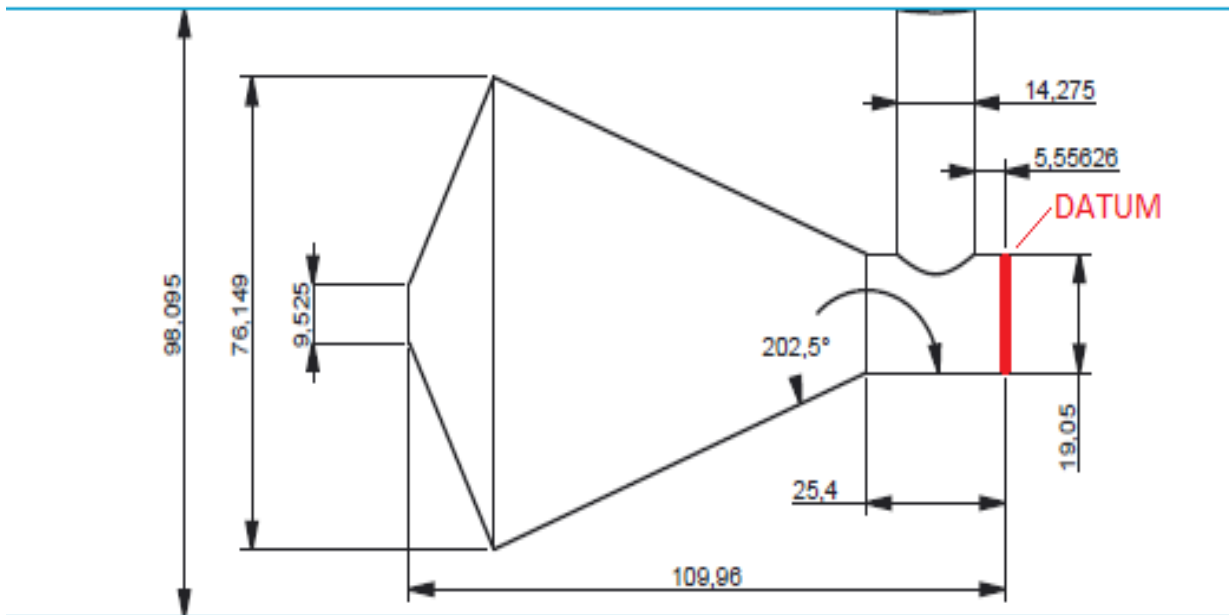
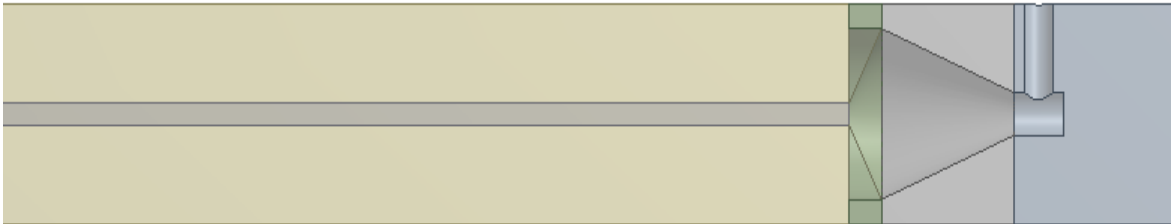
- **Zhu** – RANS- $k\epsilon$  ( $\approx 7\%$ ) and LES ( $\approx 1.54\%$ )

W. Zhu, J. Meng and Z. Yin, “3-D Numerical Simulation and Analysis on V-cone flowmeter based on LES method,” *Applied Mechanics and Materials*, Vols. 88-89, pp. 408-412, 2011.

# Flow Model

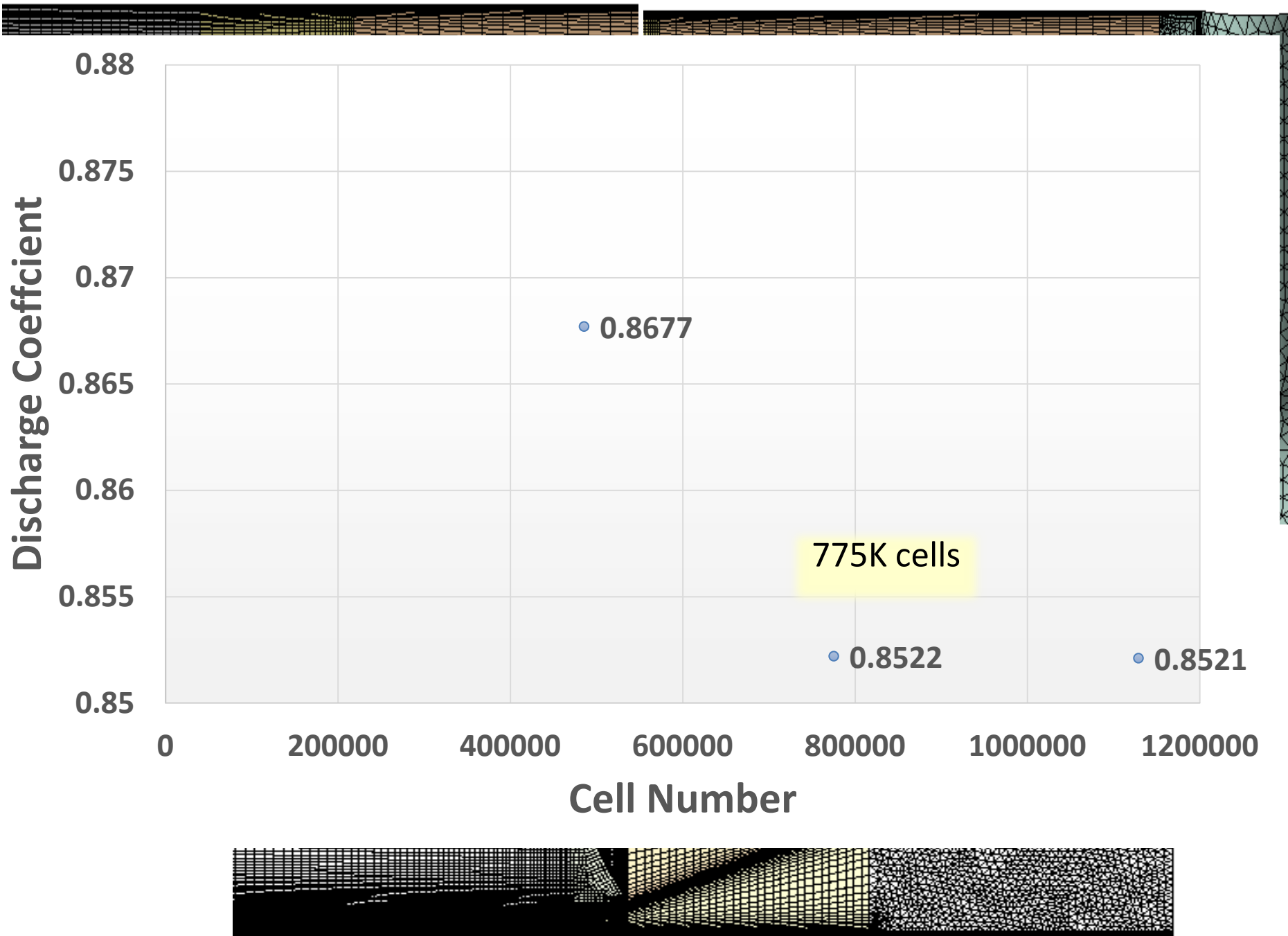
- **Reynolds Averaged Navier-Stokes (RANS)** – time independent
- **Geometry** – Three dimensional ( symmetric half model)
- **Fluid**- Air with ideal gas equation
- **Solver**- compressible density based solver
- **Turbulence Model**- RNG k- $\epsilon$  Model 2.5% variation between k- $\epsilon$  models ( standard, k-w, RNG k-w, SS k-w) with RNG- k- $\epsilon$  most accurate
- **Boundary Conditions** : Fixed inlet flow and pressure outlet
- **Wall boundary**- Standard Wall Functions 2.% variation between wall models (standard, scalable, Enhanced) with standard being most accurate

# Geometry and Mesh Representations



## Key Dimensions

$D_{\text{pipe}}$	98 mm
$D_{\text{cone}}$	76.5 mm
$\beta$	0.63
Length	110 mm

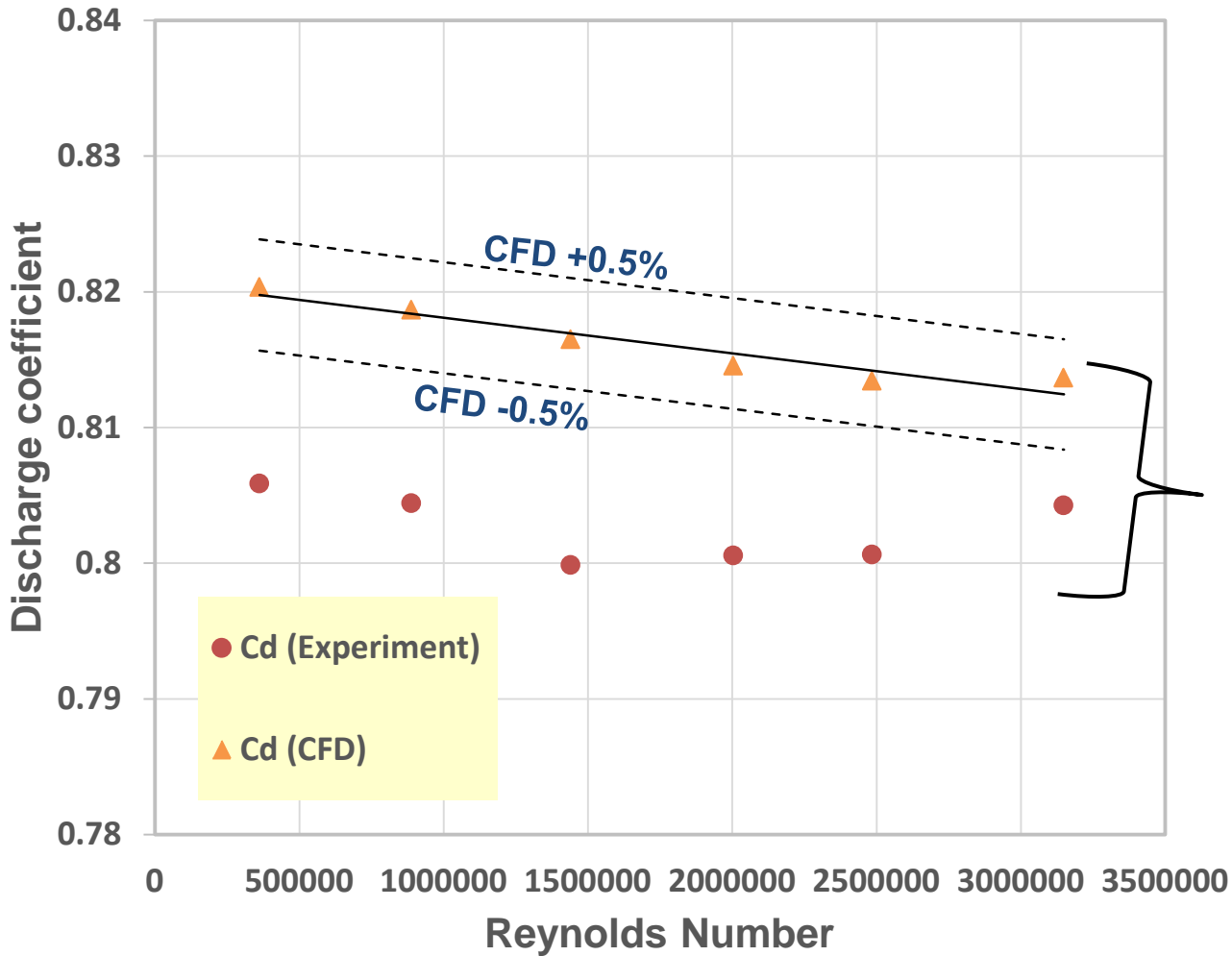




# TEST CONDITIONS

Reynold's Number	Inlet Pressure	Inlet Density	Mass Flow	Inlet Speed
	Pa	kg/m <sup>3</sup>	kg/s	m/s
<b>362390</b>	1725965	20.632	0.517	3.314
<b>888490</b>	1727688	20.685	1.265	8.095
<b>1441300</b>	1727500	20.595	2.059	13.226
<b>2004000</b>	1729343	20.336	2.891	18.814
<b>2484600</b>	1730860	20.337	3.587	23.339
<b>3148900</b>	1726240	20.765	4.470	28.482

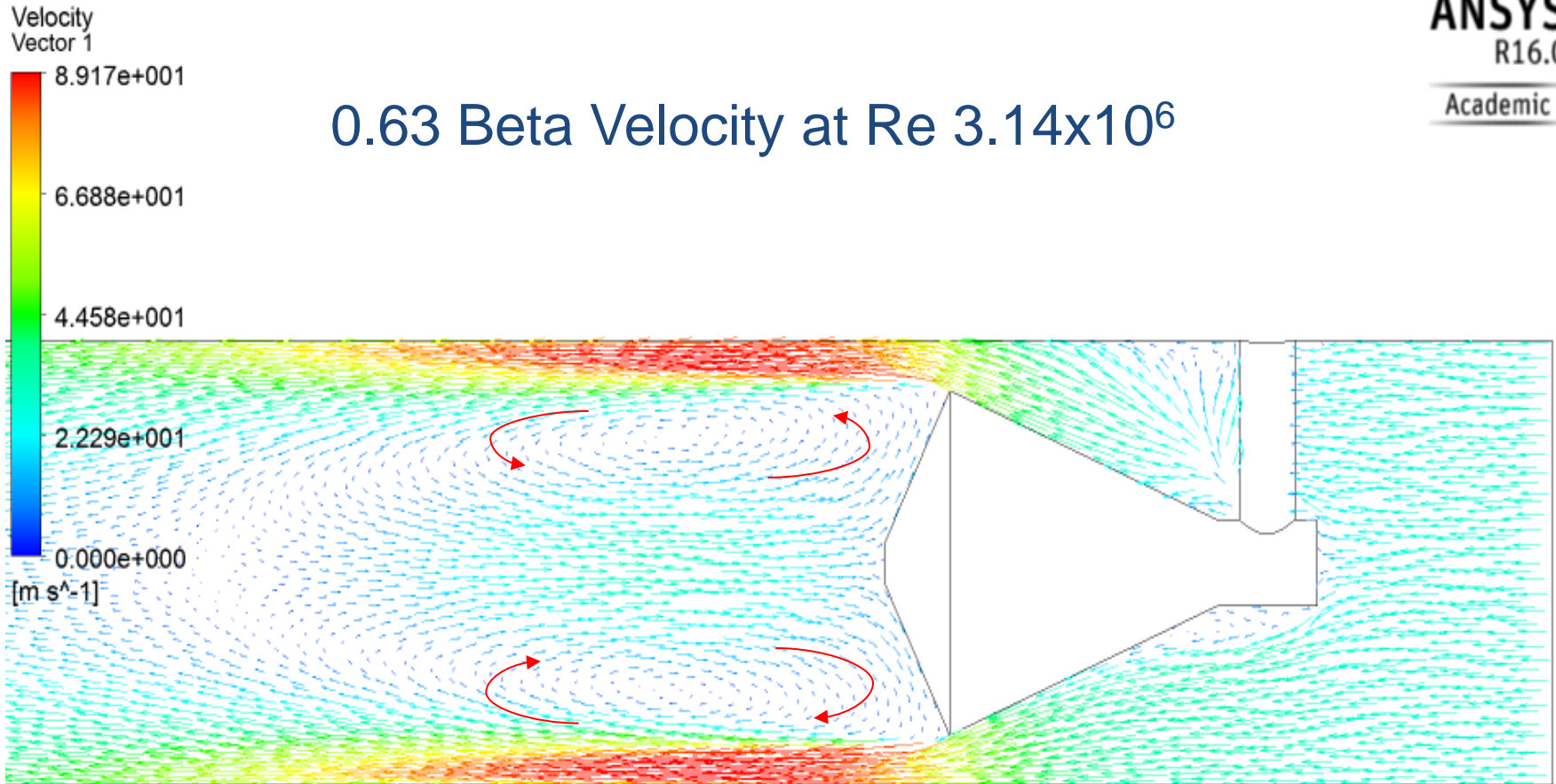
# RESULTS



Reynolds Number [E+05]	Discharge Coefficient	CD error (%)
<b>3.62</b>	0.8203	1.79
<b>8.89</b>	0.8187	1.77
<b>14.41</b>	0.8165	2.08
<b>20.04</b>	0.8145	1.74
<b>24.85</b>	0.8134	1.60
<b>31.49</b>	0.8137	1.17

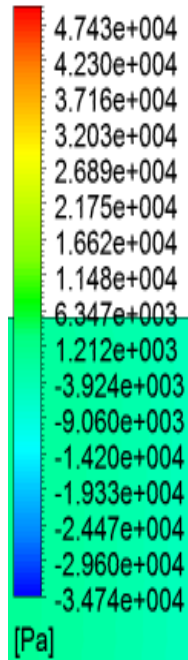
# DETAILED RESULTS - VELOCITY

0.63 Beta Velocity at  $Re\ 3.14 \times 10^6$

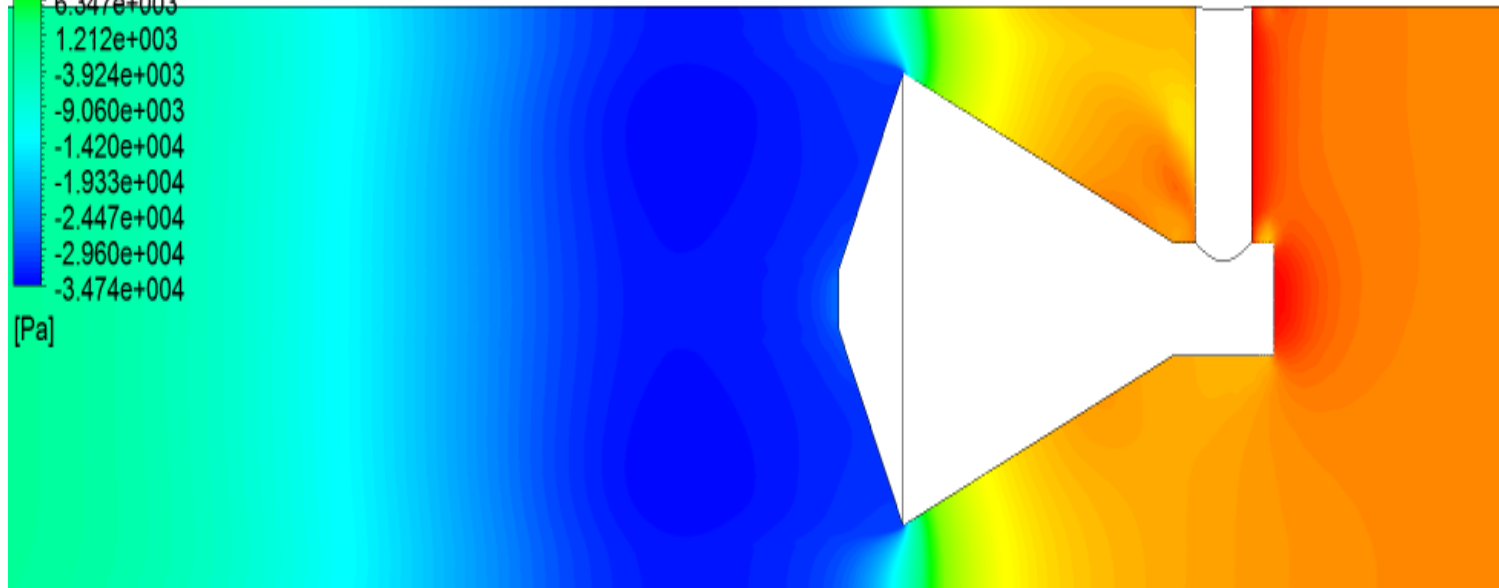


# DETAILED RESULTS - Pressure

Pressure  
Contour 1



0.63 Beta Velocity at  $Re\ 3.14 \times 10^6$



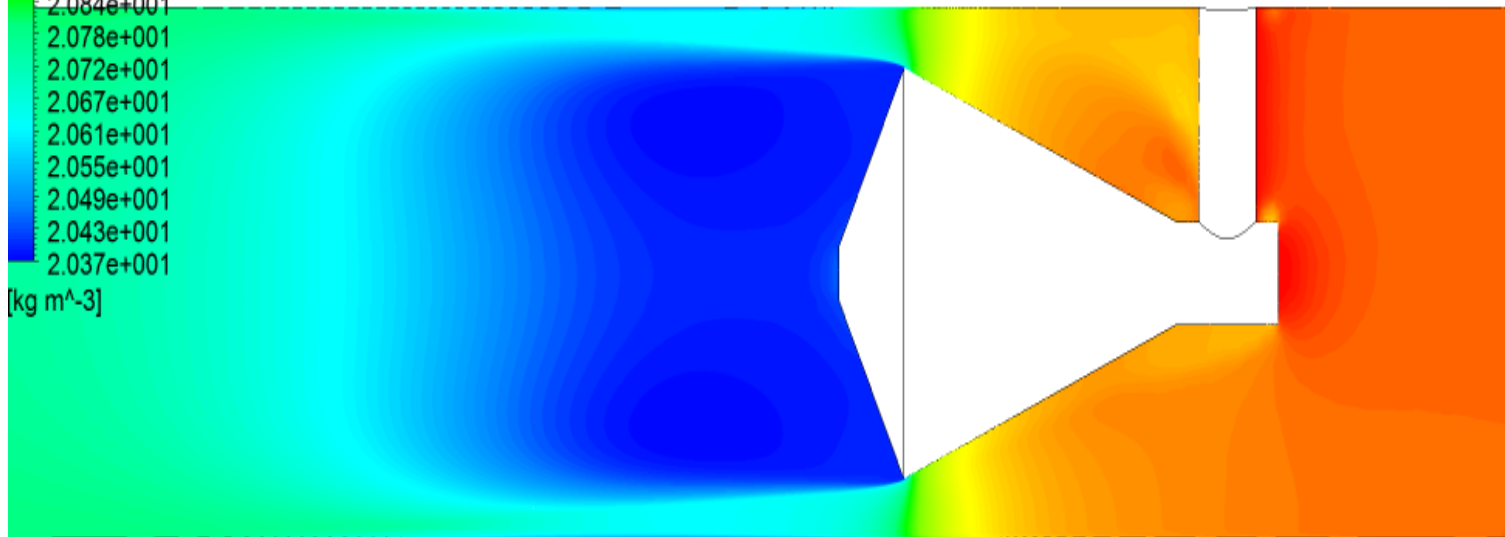
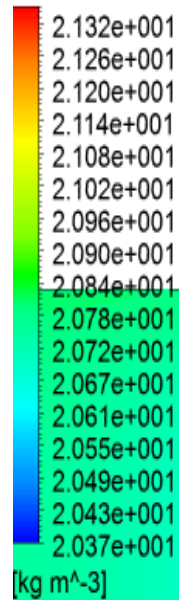
# Points to note - compressibility

Compressibility effects need to be accounted for .

Contribute  $\sim 2\%$  to  $C_d$

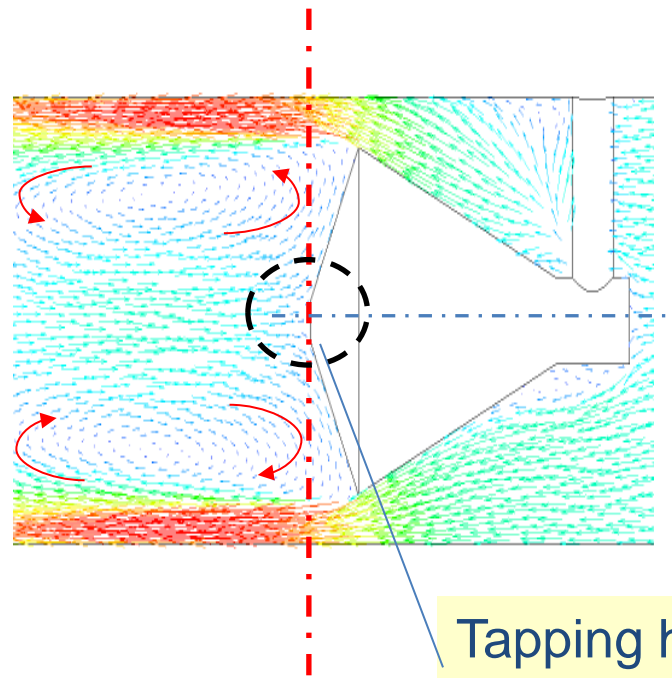
**ANSYS**  
R16.0  
Academic

Density  
Contour 1



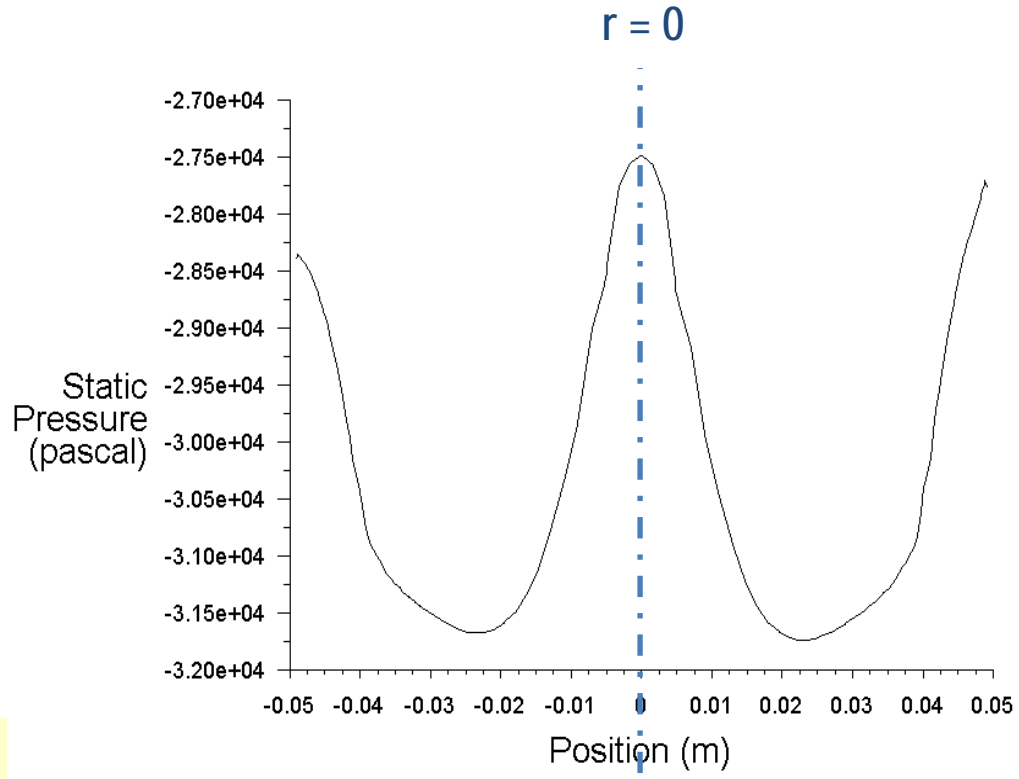
# Points to note-

## Dowstream pressure profile /tappings



$r = 0$

Tapping holes  
not modelled –  
may need to  
be



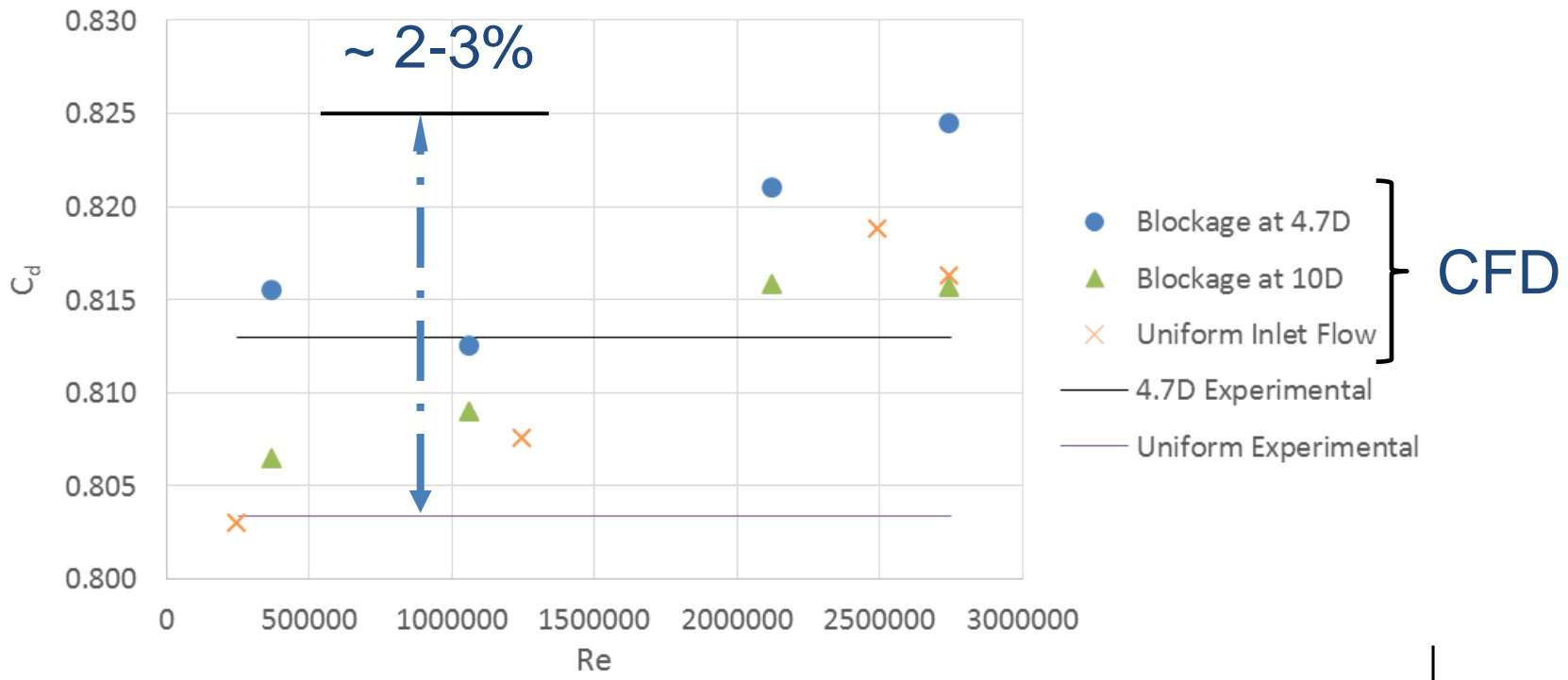
**Pressure variation across plane**

# Conclusions

- Steady RANS with RNG k-e models can predict  $C_d$  coefficients for Cones Meters to  $< 2\%$
- The dependency of the  $C_d$  on Reynolds Number can be predicted reasonably correctly.
- It is speculated that additional accuracy may be achieved by considering detailed modelling of downstream pressure tapping

# Final note

Can CFD predict  $C_d$  for non uniform upstream flows  
As accurately as for uniform inlet conditions ?

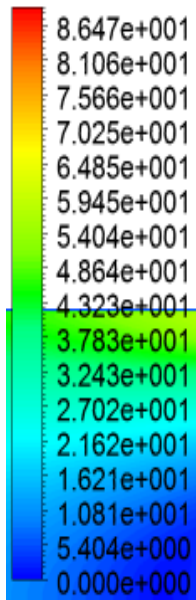


Preliminary results – say yes

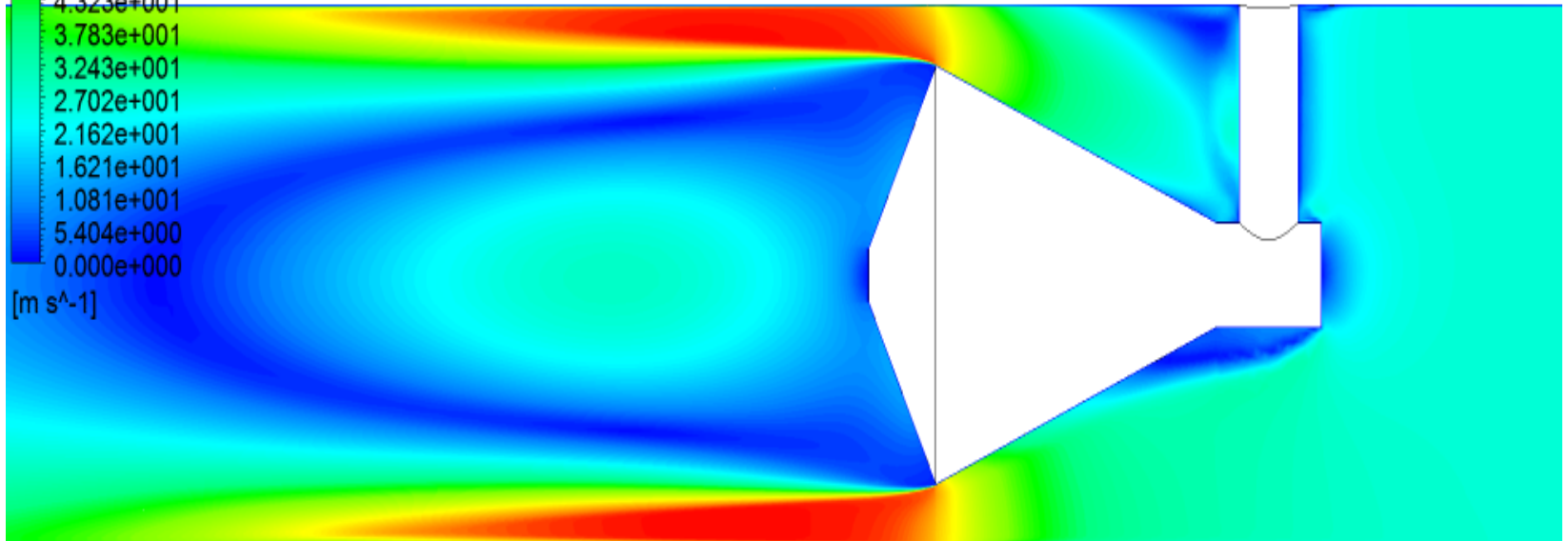


# DETAILED RESULTS

Velocity  
Contour 1



0.63 Beta Velocity at  $Re\ 3.14 \times 10^6$



[m s<sup>-1</sup>]

# ABSTRACT

Cone meters , a differential pressure flow meter device have been found to be resilient to upstream flow disturbances and hence more suitable for complex pipe geometries than traditional differential meters such orifice plates and venturi nozzles.

In this paper the computational fluid dynamic modelling of a Cone meter is studied and the ability to accurately predict the flow meter discharge coefficients is presented. The open literature suggests that prediction can be achieved to 4-5 % using RANS based two equation turbulence models and that greater accuracy to < 2% require using LES techniques. In this paper a 4" Cone , beta ratio 0.63 is studied over a Reynolds number range of  $3.6 \times 10^5$  –  $3.14 \times 10^6$  in a pressurised gas flow line.

This paper will show that by appropriate meshing and accounting for compressibility that RANs based approaches can achieve an accuracy of less than 2%, establishing CFD as a suitable vehicle for flow meter design.